

Wheel Mass to Body Ratio

by Erik Waelchli





The Questions

One Unit of Wheel Weight is "worth" how much Body Weight?

- Internet research reveals claims of ratios from 2 to 10 times!
- Are these figures for real?
- What are the factors that influence this ratio?



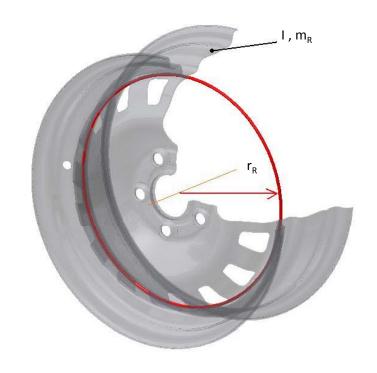
The Wheel-Rim Mass Radius

The need for a simple model

$$I = m \times r^2$$

 Concentrate the wheel mass to the "Mass Radius"

$$r_R = \sqrt[2]{I_{wheel}/m_{wheel}}$$





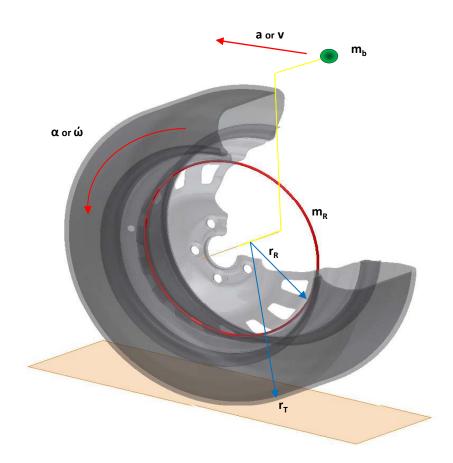
Physics & "The Relationship"

$$m_B / m_R = 1 + r_R^2 / r_T^2$$

i.e. the Mass-Ratio

or
$$m_B = m_R \times (1 + r_R^2/r_T^2)$$

or
$$m_R = m_R / (1 + r_R^2/r_T^2)$$





Numerical Limits and Ranges

$$m_B / m_R = 1 + r_R^2 / r_T^2$$

- Minimum Limit
- Maximum Limit

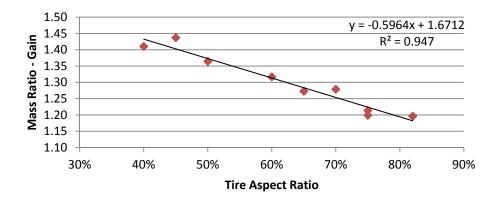
- $m_B/m_R = 1.0$
- $m_R/m_R = 2.0$
- Typical Range for Wheels $m_B / m_R =$ dependant on aspect ratio of tire

$$m_B / m_R = 1.2 ... 1.5$$



"Rotating-to-Body Mass Ratio" Comparison with different Tire Aspect Ratios

| Vehicle | | Corvette | Camaro | Cadillac STS | Pass-Car | Silverado | Pass-Car | Hummer H3 |
|---------------------------------------|-----|-------------|-------------|--------------|------------|------------|------------|------------|
| Rim | | 18 x 8.5 | 20 x 8 | 18 x 8 | J14 x 5.5 | J8 x 18 | J14 x 5.5 | 16 x 7.5 |
| Tire | | P245/40ZR18 | P245/45ZR20 | P235/50ZR18 | P185/60R14 | P265/65R18 | P185/70R14 | P265/75R16 |
| Aspect Ratio | | 40% | 45% | 50% | 60% | 65% | 70% | 75% |
| Tire Rolling Radius | mm | 306.9 | 330.4 | 325.7 | 271.7 | 376.5 | 289.5 | 377.9 |
| Wheel-Rim Mass Radius | mm | 196.6 | 218.4 | 196.6 | 152.9 | 196.6 | 152.9 | 174.8 |
| Mass Ratio = $1 + R_p^2 / R_{\tau}^2$ | [-] | 1.41 | 1.44 | 1.36 | 1.32 | 1.27 | 1.28 | 1.21 |





The interesting Weight is Outside

| | | Original | Outer Section | Inner Section | |
|-----------------------------------|--------------------------------|----------|----------------------|---------------|--------|
| Inertia | 1 | 138,783 | 128,938 | 137,302 | kg-mm² |
| Wheel Mass | m_{R} | 5.86 | 5.61 | 5.61 | kg |
| Delta Wheel Mass | dm_R | | 0.250 | 0.250 | kg |
| Mass Radius Tire Radius | r_R | 153.9 | 151.6 | 156.44 | mm |
| | r_{T} | 266 | 266 | 266 | mm |
| Ratio | m _B /m _R | 1.335 | 1.325 | 1.346 | [-] |
| Wheel Mass ref Delta equiv. Bo | • | 7.82 | 7.43 0.389 | 7.55 0.271 | |
| %-age Gain to | delta Whe | el Mass | 55.7% | 8.4% | |



The Answers

How much more is One Unit of Wheel Weight "worth" than Body Weight is influenced by:

- Where the Weight is on the Wheel
 - How far away is the wheel-mass from the wheel's rotational axis
- Aspect Ratio of the Tire
 - How far way is the wheel-mass from the road
- Typical Wheel-Mass-to-Body Ratio $m_B/m_R = 1.2$ to 1.6
 - Possible Mass Gains from 20% to 60%

 i.e. (factors of > 2 are false!)



for Feedback and Questions contact

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